

Annuities: Investments + Loans

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- Investments:
- ① Savings Accounts .05% - 1%
 - ② Term Deposits 2 - 3%
 - ③ Bonds 2 - 4%
 - ④ Mutual Funds - pool \$ with other investors & an expert buys stocks.
 - ⑤ Stocks (Shares)
 - ⑥ RESP - registered education savings plan
RRSP - registered retirement savings plan

- Loans
- ① Credit Card 20%
 - ② Line of Credit prime + 4%
3.5
 - ③ Student Loans (6 - 9%)
 - ④ Car loans
 - ⑤ Mortgages.

You put \$100/mo in a RRSP that earns 5% interest compounded monthly. How much would you have after 2 years.

$$A = \frac{R [(1+i)^n - 1]}{i}$$

A = amount in \$ (FV future value for investments)

R = amount you regularly invest
 (or pay)
 i = interest rate per compounding
 period (in decimal)
 n = # of deposits / payments

$$A = \frac{R [(1+i)^n - 1]}{i}$$

$$A = \frac{100 \left[\left(1 + \frac{.05}{12}\right)^{24} - 1 \right]}{\frac{.05}{12}}$$

$$A = \frac{100 [(1.041\bar{6})^{24} - 1]}{.041\bar{6}}$$

$$A = 2518.59 \quad 24 \times 100 = 2400$$

Say you want to retire at 65 with
 1,000,000. At age 25 you start
 investing in a mutual fund that
 pays 4% ^{compounded monthly}. How much should you
 deposit monthly to reach your goal?

$$A = \frac{R [(1+i)^n - 1]}{i}$$

$$1,000,000 = \frac{R \left[\left(1 + \frac{.04}{12}\right)^{480} - 1 \right]}{\frac{.04}{12}}$$

$$(.00\bar{3}) 1,000,000 = \frac{R [(1.00\bar{3})^{480} - 1]}{.00\bar{3}} \quad (.00\bar{3})$$

$$\frac{3333.3\bar{3}}{3.93987} = \frac{R [3.93987]}{3.93987}$$

$$\$846.05 = R$$

With loans $A = PV$ (present value)

$$PV = \frac{R [1 - (1+i)^{-n}]}{i}$$

$n = \#$ of payments.

Eg You buy a TV + pay \$80/mo for 36 months @ 10% compounded monthly. Find PV (total that you owe).

$$PV = \frac{80 [1 - (1 + \frac{.10}{12})^{-36}]}{\frac{.10}{12}}$$

$$PV = 2479.30$$

$$36 \times 80 = \underline{2880}$$

$$2880 - 2479.30 = \\ \$400.70 \text{ interest}$$

Mortgage is a loan for property / house
All mortgages in Canada are compounded semi-annually but are usually paid monthly, semi-monthly or bi-weekly. To adjust for the formula where compounded / payment periods are different the interest is adjusted.

This converted rate is called the effective interest rate.

You get a mortgage of \$400,000 for 25 years with an effective interest rate of

3.9% compounded monthly. What is the monthly payment.

$$PV = \frac{R(1 - (1+i)^{-n})}{i}$$

$$400,000 = \frac{R(1 - (1 + \frac{.039}{12})^{-300})}{\frac{.039}{12}}$$

$$400,000 = \frac{R(1 - (1.00325)^{-300})}{.00325}$$

$$\frac{1300}{.6222} = \frac{R(.6222)}{.00325}$$

$$\$2089.32 = R$$

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$$\textcircled{6} \quad 7000 = \frac{R((1 + \frac{.0195}{4})^{20} - 1)}{\frac{.0195}{4}}$$

CMHC Fees.

Canadian Mortgage + Housing Corporation.

5% - 7.99% → 4% fee

$$100,000 + 4000 = 104,000$$