Pre-Calc 11 Unit 1 Pre-test

Questions #1-20 should be done without a calculator.

- 1. Which of the following numbers is irrational?

C. $\sqrt{\frac{1}{9}}$

- **D.** $\sqrt{\frac{24}{4}}$
- 2. Evaluate $125^{\frac{1}{3}}$ without using a calculator.
- **B.** 11.18
- **C.** -5
- **D.** $41\frac{2}{3}$

- 3. Write $43^{\frac{3}{2}}$ as a radical.
 - **A.** $(\sqrt[3]{43})^2$ **B.** $(\sqrt{43})^3$
- **C.** $\sqrt[1.5]{43}$
- **D.** $\sqrt[3]{43^2}$

- **4.** Write $\sqrt{\left(\frac{5}{2}\right)^7}$ as a power.
 - **A.** $\left(\frac{5}{2}\right)^{-\frac{7}{2}}$ **B.** $\left(\frac{5}{2}\right)^{\frac{2}{7}}$ **C.** $\left(\frac{2}{5}\right)^{-\frac{2}{7}}$ **D.** $\left(\frac{5}{2}\right)^{\frac{7}{2}}$

- **5.** Evaluate $(-243)^{0.6}$.
 - **A.** −27
 - **B.** 27

- **C.** 9462.5994...
- D. does not exist

- **6.** Evaluate $4^{2.5}$.
 - **A.** 18
 - **B.** 32

- **C.** 1.741 101...
- **D.** 40
- 7. Evaluate $8^{-\frac{4}{3}}$ without using a calculator.
- C. $\frac{1}{16}$
- **D.** −16

- **8.** Evaluate $49^{-0.5}$ without using a calculator.
- C. $\frac{1}{7}$
- **D.** 7

- **9.** Simplify $(27a^6b^9)^{\frac{2}{3}}$. **A.** $9a^9b^6$
- **B.** $27a^4b^6$
- **C.** $9a^4b^6$ **D.** $9a^4b^9$

- **10.** Evaluate $\frac{0.64^{\frac{5}{2}}}{0.64^4}$.
- **B.** 18.1899...

- **11.** Evaluate: $\sqrt{(-9-(-17))^2}$
- **B.** 2.83
- **C.** 8
- **D.** 64

- **12.** Which expression cannot be evaluated?
 - **A.** $\sqrt[3]{-81}$

- 13. Write this mixed radical as an entire radical: $-7\sqrt{2}$
- **B.** $\sqrt{-14}$
- **D.** $\sqrt{196}$

- **14.** Write this mixed radical as an entire radical: $-\frac{4}{3}\sqrt[3]{\frac{5}{6}}$
- **B.** $\sqrt[3]{-\frac{160}{81}}$ **C.** $\sqrt[3]{\frac{81}{160}}$
- **D.** $\sqrt[3]{41}$

- **15.** Write this entire radical as a mixed radical: $\sqrt{150}$
 - **A.** $10\sqrt{6}$
- **B.** $10\sqrt{12}$
- **C.** $5\sqrt{36}$
- **D.** $5\sqrt{6}$

- **16.** Write this entire radical as a mixed radical: $\sqrt[4]{80}$
 - **A.** $4\sqrt[4]{10}$
- **B.** $2\sqrt[4]{25}$
- C. $2\sqrt[4]{5}$
- **D.** $4\sqrt[4]{5}$

- 17. Write this entire radical as a mixed radical: $\sqrt[3]{-\frac{54}{125}}$
- C. $-\frac{5\sqrt[3]{2}}{2}$
- **D.** $-\frac{3\sqrt[3]{2}}{5}$
- **18.** For which values of the variable, x, is this radical defined? $\sqrt{-38x^3}$
 - $\mathbf{A.} \quad x \le 0$

 $\mathbf{C.} \quad x \ge 0$

B. $x \in \mathbb{R}$

- **D.** x < 0
- **19.** Write this radical in simplest form: $\sqrt{63a^9b^8}$
 - Then state the values of the variables, a and b, for which the radical is defined.
- **C.** $3ab\sqrt{7a^4b^4}$; $a \in \mathbb{R}, b \ge 0$
- **A.** $3a^4b^4\sqrt{7a}$; $a \in \mathbb{R}$, $b \ge 0$ **B.** $3ab\sqrt{7a^4b^4}$; $a \ge 0$, $b \in \mathbb{R}$
- **D.** $3a^4b^4\sqrt{7a}$; $a \ge 0, b \in \mathbb{R}$

20. For which values of the variable, x, is this radical defined?

$$\sqrt{-22x^4}$$

$$\mathbf{A.} \quad x \ge 0$$

$$\mathbf{C.} \quad x \le 0$$

B.
$$x \in \mathbb{R}$$

D.
$$x = 0$$

21. Write this radical in simplest form: $\sqrt[4]{\frac{625y^5}{512}}$

Then state the values of the variable, y, for which the radical is defined.

A.
$$\frac{5y}{2} \sqrt[4]{\frac{y}{2}}; y \ge 0$$

C.
$$\frac{5y}{4} \sqrt[4]{\frac{y}{2}}; y \ge 0$$

$$\mathbf{B.} \quad \frac{5y}{4} \sqrt[4]{\frac{1}{2}}; y \in \mathbb{R}$$

D.
$$\frac{y}{4} \sqrt[4]{\frac{5y}{2}}$$
; $y \ge 0$

22. Simplify: $\left(\frac{\frac{5}{8}^{\frac{5}{6}}}{\frac{\frac{2}{3}}{8^{\frac{4}{9}}} \frac{4}{9}}\right)^{6}$

C.
$$\frac{1}{32}$$

23. Arrange these radicals in order from greatest to least.

i)
$$3\sqrt[3]{5}$$

ii)
$$\sqrt[3]{375}$$

iii)
$$4\sqrt[3]{3}$$

iv)
$$\sqrt[3]{40}$$

24. Which statement is true?

i)
$$\sqrt{-475x^7} = (-5x^3)\sqrt{19x}$$
; for $x \in \mathbb{R}$

ii)
$$\sqrt{-475x^7} = 5|x^3|\sqrt{-19x}$$
; for $x \le 0$

iii)
$$\sqrt{-475x^7} = 5|x^3|\sqrt{-19x}$$
; for $x \ge 0$

iv) There are no values of
$$x \in \mathbb{R}$$
 for which $\sqrt{-475x^7} = 5|x^3|\sqrt{-19x}$

25. Which radical expression simplifies to $9\sqrt{2}$?

A.
$$\sqrt{32} - 7\sqrt{2} + \sqrt{8}$$

C.
$$\sqrt{32} + 7\sqrt{8} - \sqrt{2}$$

D. $\sqrt{2} + 7\sqrt{8} - \sqrt{32}$

B.
$$\sqrt{32} - \sqrt{8} + 7\sqrt{2}$$

D.
$$\sqrt{2} + 7\sqrt{8} - \sqrt{32}$$

26. Which radical expression simplifies to $-9\sqrt{x}$?

A.
$$-8\sqrt{x} + 4\sqrt{x} - 5\sqrt{x}, x \ge 0$$

C.
$$-8\sqrt{x} - 4\sqrt{x} + 5\sqrt{x}, x \ge 0$$

B.
$$-8\sqrt{x} + 4\sqrt{x} - 5\sqrt{x}, x \in \mathbb{R}$$

$$\mathbf{D.} \quad -8\sqrt{x} - 4\sqrt{x} + 5\sqrt{x}, x \in \mathbb{R}$$

- 27. Simplify by adding or subtracting like terms: $8\sqrt{13} 7\sqrt{13} + 5\sqrt{13}$
 - **A.** $6\sqrt{13}$
- C. $10\sqrt{13}$
- **D.** $6\sqrt{10}$
- **28.** Simplify by adding or subtracting like terms: $\sqrt{243} + 4\sqrt{3} \sqrt{27}$
- **B.** $8\sqrt{3}$
- **D.** 0
- **29.** Simplify by adding or subtracting like terms: $\sqrt{729} \sqrt[3]{8} \sqrt{81} + \sqrt[3]{512}$
 - **A.** $18-6\sqrt[3]{2}$

C. $18\sqrt{3} - 6\sqrt[3]{2}$

B. $6-18\sqrt{3}$

- **D**. 24
- **30.** Simplify by adding or subtracting like terms: $\sqrt[3]{729w^4} 3w\sqrt[3]{w} \sqrt[3]{27w^7} + 3w^2$, $w \in \mathbb{R}$
 - **A.** $6w\sqrt[3]{w} 3w^2\sqrt[3]{w} + 3w^2$
- C. $6w\sqrt[3]{w}$

B. $6w\sqrt[3]{w} + 6w^2$

- **D.** $3w^{3}\sqrt{w} + 3w^{2}$
- **31.** Expand and simplify this expression: $\sqrt{3}(\sqrt{2}+4)$
 - **A.** $3\sqrt{2} + 4\sqrt{3}$

C. $\sqrt{6} + \sqrt{12}$

B. $2\sqrt{3} + \sqrt{12}$

- **D.** $\sqrt{6} + 4\sqrt{3}$
- **32.** Expand and simplify this expression: $(\sqrt{5} + 7)^2$
 - **A.** $54 + 14\sqrt{5}$

C. $5\sqrt{5} + 49$

B. $5\sqrt{5} + 14\sqrt{5} + 54$

- **D.** $54 + 5\sqrt{14}$
- **33.** Rationalize the denominator: $\frac{7}{7\sqrt{5}}$

- A. $\frac{7\sqrt{5}}{35}$ B. $\frac{35\sqrt{5}}{5}$ C. $\frac{7\sqrt{5}}{5}$ D. $\frac{49\sqrt{5}}{7}$
- **34.** Expand and simplify this expression: $\left(-5\sqrt{5} 2\sqrt{3}\right)\left(4\sqrt{5} + 8\right) + 2\sqrt{5}\left(3\sqrt{5} + 3\sqrt{3}\right)$
 - A. $-70 58\sqrt{15}$
 - **B.** $-130-40\sqrt{5}+16\sqrt{3}-2\sqrt{15}$
 - C. $-70-40\sqrt{5}-16\sqrt{3}-2\sqrt{15}$
 - **D.** $-130-40\sqrt{5}-16\sqrt{3}-14\sqrt{15}$
- **35.** Expand and simplify this expression: $(2\sqrt{s} 7\sqrt{t})(5\sqrt{s} 7\sqrt{t})$, $s \ge 0$, $t \ge 0$
 - **A.** $10s 49\sqrt{st} + 49t$

C. $10s - 70\sqrt{st} + 49t$

B. $10s - 28\sqrt{st} + 49t$

- **D.** $-45st 49\sqrt{st}$
- **36.** Simplify this expression: $\frac{-9\sqrt{5}-3}{\sqrt{5}}$
 - A. $\frac{-45-3\sqrt{5}}{5}$

C. $\frac{-9-15\sqrt{5}}{5}$

B. $-225 - 3\sqrt{5}$

D. $\frac{-45\sqrt{5}-15}{5}$

- 37. Simplify this expression: $\frac{2\sqrt{3} + 9\sqrt{7}}{\sqrt{2} 8}$
 - **A.** $\frac{-2\sqrt{3} 18\sqrt{42} 72\sqrt{7}}{-6}$
 - **B.** $\frac{-2\sqrt{6} 9\sqrt{14} 16\sqrt{3} 72\sqrt{7}}{62}$
 - C. $\frac{-2\sqrt{3} 18\sqrt{42} 72\sqrt{7}}{62}$
 - **D.** $\frac{-2\sqrt{6} 9\sqrt{14} 16\sqrt{3} 72\sqrt{7}}{-6}$
- **38.** Simplify this expression: $\frac{\sqrt{7}}{\sqrt{12}} \left(\frac{-7\sqrt{3}}{\sqrt{28}}\right)$
 - **A.** $\frac{2\sqrt{21}}{3}$
- **B.** $\frac{\sqrt{2}}{3}$
- C. $\frac{2\sqrt{21}}{7}$
- **D.** $\frac{21\sqrt{2}}{11}$

- **39.** Solve this equation: $9\sqrt{4x} = 72$
 - **A.** x = 16
- **B.** x = 64
- **C.** $x = \frac{1}{8}$
- **D.** x = 8

- **40.** Solve this equation: $9\sqrt{x} 6 = 30$
 - $\mathbf{A.} \quad x = 4$
- **B.** x = 16
- **C.** x = 9
- **D.** x = 8

- **41.** Solve this equation: $\sqrt{-2+8x} = \sqrt{-44+2x}$
 - **A.** $x = \frac{1}{7}$
- **B.** x = -5
- **C.** x = -6
- **D.** no real solution

- **42.** Solve this equation: $\frac{\sqrt{x}}{3} = 4$
 - **A.** x = 144
- **B.** x = 12
- **C.** x = 7
- **D.** x = 3

- **43.** Solve this equation: $5 = \sqrt[5]{5x 8} + 3$
 - **A.** x = -8
- **B.** $x = \frac{32}{5}$
- **C.** x = 40
- **D.** x = 8
- 44. Is the following number rational or irrational? Justify your answer!

 $\sqrt{\frac{10}{160}}$

45. Evaluate $\left(\frac{8}{27}\right)^{-\frac{2}{3}}$ without using a calculator.



46. Simplify $\left(\frac{w^{-15}y^{12}}{-64x^3}\right)^{-\frac{1}{3}}$.



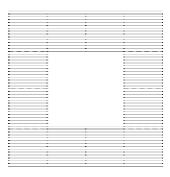
47. Simplify: $\left(9^{\frac{1}{2}} + 9^{\frac{-1}{2}}\right)^{-3}$



48. When 8 is added to an integer, *x*, the absolute value of the sum is 5. Determine a value for *x*. How many different values of *x* are possible? Show how you solved the problem.

- **49.** Sixteen congruent squares are placed together to form a large square. The 4 middle squares are removed. The final shape is a square within a square. The area of the large square is 80 square units.
 - a) What is the area of the inner square?
 - b) What is the difference between the perimeters of the outer square and the inner square?

Explain your work.



50. Expand and simplify this expression: $\left(-5\sqrt{2} + 3\sqrt{3}\right)\left(-6\sqrt{2} - 2\sqrt{3}\right)$ Show your work.

- **51.** a) Identify the values of the variables for which this expression is defined.
 - b) Write the expression in simplest form. Show your work.

$$\frac{-5\sqrt{s} + 3\sqrt{t}}{4\sqrt{s} - 5\sqrt{t}}$$

52. Determine whether the given value of x is a root of this equation. Justify your answer. $\sqrt{5x-5} = \sqrt{6x-8}$; x = 9

53. Does this equation have a real root? If so, determine its value. $6 = \sqrt{8 - 7x}$

$$6 = \sqrt{8 - 7x}$$

54. Solve this equation: $4\sqrt{2x-2} = 2\sqrt{5x+4}$

Questions #1-20 should be done without a calculator. Answer Section

1.	ANS:	D	PTS:	1				
	ANS:		PTS:		DIF:	Easy	REF.	4.4 Fractional Exponents and Radicals
		10.AN3		Algebra and N		Lusy		Conceptual Understanding
3.	ANS:	В	PTS:	•	DIF:	Easy		4.4 Fractional Exponents and Radicals
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4.	ANS:	D	PTS:	~	DIF:	Easy		4.4 Fractional Exponents and Radicals
	LOC:	10.AN3	TOP:	Algebra and N	lumber	·		Conceptual Understanding
5.	ANS:	A	PTS:	1	DIF:	Moderate	REF:	4.4 Fractional Exponents and Radicals
	LOC:	10.AN3	TOP:	Algebra and N	lumber		KEY:	Conceptual Understanding
6.	ANS:		PTS:			Moderate		4.4 Fractional Exponents and Radicals
		10.AN3		Algebra and N				Conceptual Understanding
7.	ANS:		PTS:		DIF:	Easy		4.5 Negative Exponents and Reciprocals
_		10.AN3		Algebra and N				Conceptual Understanding
8.	ANS:		PTS:			Moderate		4.5 Negative Exponents and Reciprocals
•		10.AN3		Algebra and N		.		Conceptual Understanding
9.	ANS:		PTS:		DIF:	Easy		4.6 Applying the Exponent Laws
10		10.AN3		Algebra and N		Madamata		Conceptual Understanding
10.	ANS:	10.AN3	PTS:	Algebra and N		Moderate		4.6 Applying the Exponent Laws Conceptual Understanding
11	ANS:		PTS:	-		Moderate		2.1 Absolute Value of a Real Number
11.		11.AN1		Relations and			KLI.	2.1 Absolute Value of a Real Number
		Conceptual Un						
12.	ANS:	_	PTS:	_	DIF:	-	OBJ:	Section 4.4
	NAT:	AN2	TOP:	Irrational Nun	nbers		KEY:	irrational number
13.	ANS:	C	PTS:	0	DIF:	Easy	REF:	2.2 Simplifying Radical Expressions
	LOC:	11.AN2	TOP:	Relations and	Functio	ons	KEY:	Procedural Knowledge
14.	ANS:	В	PTS:	0	DIF:	Moderate	REF:	2.2 Simplifying Radical Expressions
	LOC:	11.AN2	TOP:	Relations and	Functio	ons	KEY:	Procedural Knowledge
15.	ANS:		PTS:		DIF:	•		2.2 Simplifying Radical Expressions
		11.AN2		Relations and				Procedural Knowledge
16.	ANS:		PTS:			Moderate		2.2 Simplifying Radical Expressions
4-		11.AN2		Relations and				Procedural Knowledge
17.	ANS:		PTS:			Moderate		2.2 Simplifying Radical Expressions
10		11.AN2		Relations and				Procedural Knowledge
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19.	ANS:	•	PTS:	•		Difficult	REF.	2.2 Simplifying Radical Expressions
17.		11.AN2		Relations and			TLLI .	2.2 Simplifying Rudious Empressions
		Conceptual Understanding Procedural Knowledge						
20.		-	PTS:	-		Moderate	REF:	2.2 Simplifying Radical Expressions
	LOC:	11.AN2	TOP:	Relations and				
	KEY:	Conceptual Understanding Procedural Knowledge						

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21. ANS: C
                       PTS: 0
                                          DIF: Difficult
                                                              REF: 2.2 Simplifying Radical Expressions
    LOC: 11.AN2
                       TOP: Relations and Functions
    KEY: Conceptual Understanding | Procedural Knowledge
22. ANS: C
                       PTS: 1
23. ANS: B
                       PTS: 0
                                           DIF: Moderate
                                                              REF: 2.2 Simplifying Radical Expressions
    LOC: 11.AN2
                       TOP: Relations and Functions
                                                              KEY: Procedural Knowledge
24. ANS: A
                       PTS: 0
                                           DIF: Difficult
                                                              REF: 2.2 Simplifying Radical Expressions
    LOC: 11.AN2
                       TOP: Relations and Functions
    KEY: Procedural Knowledge | Conceptual Understanding
25. ANS: B
                       PTS: 0
                                           DIF:
                                                Easy
    REF: 2.3 Adding and Subtracting Radical Expressions
                                                              LOC: 11.AN2
    TOP: Relations and Functions
                                           KEY: Procedural Knowledge
26. ANS: A
                       PTS: 0
                                           DIF: Moderate
    REF: 2.3 Adding and Subtracting Radical Expressions
                                                              LOC: 11.AN2
    TOP: Relations and Functions
                                           KEY: Conceptual Understanding | Procedural Knowledge
27. ANS: A
                       PTS: 0
                                          DIF: Easy
    REF: 2.3 Adding and Subtracting Radical Expressions
                                                              LOC: 11.AN2
    TOP: Relations and Functions
                                           KEY: Procedural Knowledge
28. ANS: C
                       PTS: 0
                                           DIF: Easy
    REF: 2.3 Adding and Subtracting Radical Expressions
                                                              LOC: 11.AN2
    TOP: Relations and Functions
                                           KEY: Procedural Knowledge
29. ANS: D
                       PTS: 0
                                           DIF: Moderate
    REF: 2.3 Adding and Subtracting Radical Expressions
                                                              LOC: 11.AN2
    TOP: Relations and Functions
                                           KEY: Conceptual Understanding | Procedural Knowledge
30. ANS: A
                       PTS: 0
                                           DIF: Moderate
    REF: 2.3 Adding and Subtracting Radical Expressions
                                                              LOC: 11.AN2
    TOP: Relations and Functions
                                           KEY: Conceptual Understanding | Procedural Knowledge
31. ANS: D
                       PTS: 0
                                           DIF: Easy
    REF: 2.4 Multiplying and Dividing Radical Expressions
                                                              LOC: 11.AN2
    TOP: Relations and Functions
                                           KEY: Procedural Knowledge
32. ANS: A
                       PTS: 0
                                           DIF: Easy
    REF: 2.4 Multiplying and Dividing Radical Expressions
                                                              LOC: 11.AN2
    TOP: Relations and Functions
                                           KEY: Procedural Knowledge
33. ANS: A
                       PTS: 0
                                           DIF: Easy
    REF: 2.4 Multiplying and Dividing Radical Expressions
                                                              LOC: 11.AN2
    TOP: Relations and Functions
                                           KEY: Procedural Knowledge
34. ANS: C
                       PTS: 0
                                           DIF: Moderate
    REF: 2.4 Multiplying and Dividing Radical Expressions
                                                              LOC: 11.AN2
    TOP: Relations and Functions
                                           KEY: Conceptual Understanding | Procedural Knowledge
                                           DIF: Moderate
35. ANS: A
                       PTS: 0
    REF: 2.4 Multiplying and Dividing Radical Expressions
                                                              LOC: 11.AN2
    TOP: Relations and Functions
                                           KEY: Conceptual Understanding | Procedural Knowledge
36. ANS: A
                                           DIF: Moderate
                       PTS: 0
                                                              LOC: 11.AN2
    REF: 2.4 Multiplying and Dividing Radical Expressions
    TOP: Relations and Functions
                                           KEY: Conceptual Understanding | Procedural Knowledge
37. ANS: B
                       PTS: 0
                                           DIF: Moderate
    REF: 2.4 Multiplying and Dividing Radical Expressions
                                                              LOC: 11.AN2
    TOP: Relations and Functions
                                           KEY: Conceptual Understanding | Procedural Knowledge
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38. ANS: A PTS: 0 DIF: Difficult LOC: 11.AN2 REF: 2.4 Multiplying and Dividing Radical Expressions **TOP:** Relations and Functions KEY: Conceptual Understanding | Procedural Knowledge REF: 2.5 Solving Radical Equations **39.** ANS: A PTS: 0 LOC: 11.AN3 **TOP:** Relations and Functions KEY: Procedural Knowledge **40.** ANS: B PTS: 0 DIF: Easy REF: 2.5 Solving Radical Equations LOC: 11.AN3 **TOP:** Relations and Functions KEY: Procedural Knowledge **41.** ANS: D PTS: DIF: Moderate REF: 2.5 Solving Radical Equations **TOP:** Relations and Functions LOC: 11.AN3 KEY: Conceptual Understanding | Procedural Knowledge **42.** ANS: A PTS: 0 DIF: Moderate REF: 2.5 Solving Radical Equations LOC: 11.AN3 **TOP:** Relations and Functions KEY: Procedural Knowledge **43.** ANS: D PTS: 0 DIF: Difficult REF: 2.5 Solving Radical Equations LOC: 11.AN3 **TOP:** Relations and Functions KEY: Conceptual Understanding | Procedural Knowledge **44.** ANS: Rational because it simplifies to $\sqrt{\frac{1}{16}}$ which is a perfect square. The square root of perfect squares are rational. PTS: 1 **45.** ANS: $\frac{9}{4}$ PTS: 1 Moderate REF: 4.5 Negative Exponents and Reciprocals DIF: LOC: 10.AN3 TOP: Algebra and Number **KEY:** Conceptual Understanding **46.** ANS: PTS: 1 DIF: Moderate REF: 4.6 Applying the Exponent Laws LOC: 10.AN3 TOP: Algebra and Number **KEY**: Conceptual Understanding **47.** ANS: 27 1000 PTS: 1 **48.** ANS: Write, then solve an equation: |x + 8| = 5Since |5/ = 5 and |-5| = 5then, x + 8 = 5x + 8 = -5or x = -13x = -3So, two values of x are possible: -3 or -13

PTS: 0 DIF: Difficult REF: 2.1 Absolute Value of a Real Number

LOC: 11.AN1 TOP: Relations and Functions

KEY: Procedural Knowledge | Communication | Problem-Solving Skills

49. ANS:

a) The area of the large square is 80 square units.

So, the area of each small square is: $\frac{80}{16}$, or 5 square units.

The inner square has the area of 4 small squares: 4(5) = 20

The area of the inner square is 20 square units.

b) The side length of a small square is the square root of its area: $\sqrt{5}$ units

The perimeter of the outer square is equal to 16 times the side length of the small square:

 $16\sqrt{5}$ units

The perimeter of the inner square is equal to 8 times the side length of the small square:

 $8\sqrt{5}$

Difference between perimeters: $16\sqrt{5} - 8\sqrt{5} = 8\sqrt{5}$

The difference between the perimeters of the outer square and the inner square is $8\sqrt{5}$ units.

PTS: 0 DIF: Moderate REF: 2.3 Adding and Subtracting Radical Expressions

LOC: 11.AN2 TOP: Relations and Functions

KEY: Procedural Knowledge | Communication | Problem-Solving Skills

50. ANS:

$$(-5\sqrt{2} + 3\sqrt{3})(-6\sqrt{2} - 2\sqrt{3})$$

$$= -5\sqrt{2}(-6\sqrt{2} - 2\sqrt{3}) + 3\sqrt{3}(-6\sqrt{2} - 2\sqrt{3})$$

$$= 60 + 10\sqrt{6} - 18\sqrt{6} - 18$$

$$= 42 - 8\sqrt{6}$$

PTS: 0 DIF: Easy REF: 2.4 Multiplying and Dividing Radical Expressions

LOC: 11.AN2 TOP: Relations and Functions KEY: Procedural Knowledge | Communication

51. ANS:

a) $s \ge 0$ and $t \ge 0$

b)
$$\frac{-5\sqrt{s} + 3\sqrt{t}}{4\sqrt{s} - 5\sqrt{t}} = \frac{\left(-5\sqrt{s} + 3\sqrt{t}\right)}{\left(4\sqrt{s} - 5\sqrt{t}\right)} \cdot \frac{\left(4\sqrt{s} + 5\sqrt{t}\right)}{\left(4\sqrt{s} + 5\sqrt{t}\right)}$$
$$= \frac{-20s - 25\sqrt{st} + 12\sqrt{st} + 15t}{(4\sqrt{s})^2 - (5\sqrt{t})^2}$$
$$= \frac{-20s - 13\sqrt{st} + 15t}{16s - 25t}$$

PTS: 0 DIF: Moderate REF: 2.4 Multiplying and Dividing Radical Expressions

LOC: 11.AN2 TOP: Relations and Functions

KEY: Conceptual Understanding | Procedural Knowledge | Communication

52. ANS:

L.S. =
$$\sqrt{5x-5}$$

= $\sqrt{5(9)-5}$
= $\sqrt{40}$
R.S. = $\sqrt{6x-8}$
= $\sqrt{6(9)-8}$
= $\sqrt{46}$

Since the left side does not equal the right side, x = 9 is not a root of the equation.

PTS: 0 DIF: Easy REF: 2.5 Solving Radical Equations

LOC: 11.AN3 TOP: Relations and Functions KEY: Procedural Knowledge | Communication

53. ANS:

Since $8 - 7x \ge 0$, then $x \le 1\frac{1}{7}$

$$6 = \sqrt{8 - 7x}$$

$$6^2 = \left(\sqrt{8 - 7x}\right)^2$$

$$36 = 8 - 7x$$

$$28 = -7x$$

$$x = -4$$

Since x = -4 lies in the set of possible values for x, x = -4 is a real root.

PTS: 0 DIF: Moderate REF: 2.5 Solving Radical Equations

LOC: 11.AN3 TOP: Relations and Functions

KEY: Conceptual Understanding | Procedural Knowledge | Communication

54. ANS:

x = 4

PTS: 0 DIF: Moderate REF: 2.5 Solving Radical Equations

LOC: 11.AN3 TOP: Relations and Functions KEY: Conceptual Understanding | Procedural Knowledge